

**Unit 1 Higher Tier
Mark scheme**

Apart from questions where the mark scheme states otherwise, the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1		2.745	1	B1
				Total 1 mark

Question	Working	Answer	Mark	Notes
2	$\frac{16}{3} - \frac{20}{7} \text{ or}$ $\left(5\right) \frac{7}{21} - \left(2\right) \frac{18}{21} \text{ or } \left(5\right) \frac{7a}{21a} - \left(2\right) \frac{18a}{21a}$		3	M1 for correct improper fractions or fractional part of numbers written correctly over a common denominator
	$\frac{112}{21} - \frac{60}{21} \text{ or } \frac{112a}{21a} - \frac{60a}{21a} \text{ or } 5\frac{7}{21} - 2\frac{18}{21} = 3 - \frac{11}{21} \text{ oe}$ $\text{or } 5\frac{7}{21} - 2\frac{18}{21} = 4\frac{28}{21} - 2\frac{18}{21}$			M1 for correct fractions with a common denominator with minus sign or mixed numbers to the stage shown
	$\frac{112}{21} - \frac{60}{21} = 2\frac{10}{21} \text{ oe or}$ $3 - \frac{11}{21} = 2\frac{10}{21}$ $5\frac{7}{21} - 2\frac{18}{21} = 4\frac{28}{21} - 2\frac{18}{21} = 2\frac{10}{21}$	Shown		A1 Dep on M2 for a correct answer from fully correct working If all 3 fractions turned into improper fractions on the first line $\frac{16}{3} - \frac{20}{7} = \frac{52}{21}$ then the student clearly needs to show that the LHS = $\frac{52}{21}$
				Total 3 marks

Question	Working	Answer	Mark	Notes
3	$1 - (0.26 + 0.18)$ (= 0.56) oe or 0.28 oe or $x + x = 1 - (0.26 + 0.18)$ oe "0.28" + 0.26 (= 0.54) "0.54" \times 250 oe eg "0.28" \times 250 + 0.26×250 <i>Correct answer scores full marks (unless from obvious incorrect working).</i>	135	4	M1 0.28 oe may be seen in the table M1 adding the two required probabilities M1 for multiplying the probabilities by 250 A1
Total 4 marks				

Question	Working	Answer	Mark	Notes
4 (a)	$n^2 - 6n + 4n - 24$ <i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$n^2 - 2n - 24$	2	M1 for any 3 correct terms or for 4 out of 4 correct terms ignoring signs or for $n^2 - 2n \dots$ or for $\dots - 2n - 24$ A1 oe
(b)	$x - 12$ or $\frac{3}{4}x - \frac{5}{4}$ oe or $0.75x - 1.25$ oe $x - 3x = -5 + 12$ oe or $5x = 7$ oe or $2x - \frac{3}{4}x = -\frac{5}{4} + 3$ or $2x - 0.75x = -1.25 - 3$ oe <i>Working required</i>	$\frac{7}{5}$	3	M1 for correct multiplication by 4 or separate fractions on the RHS M1 ft (dep on 4 terms) for terms in x on one side of equation and number terms on the other A1 oe dep on M1 1.4 or $1\frac{2}{5}$
Total 5 marks				

Question	Working	Answer	Mark	Notes
5	For sight of 5 hrs 24 mins = 5.4 (hrs) or $5 \frac{24}{60} \left(= 5 \frac{2}{5} \right)$ or 324 (mins)		3	B1
	$3980 \div 5.4$ or $\frac{3980}{324} \times 60$			M1 For distance \div time that should give a speed in km/h. (SC allow $3980 \div 5.24 (= 759.5\dots)$ or 760) for this mark unless mark has been awarded for 324 minutes or 5.4 hours oe)
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	737		A1 awrt 737 (if no working shown, 738 gets SCB2)
				Total 3 marks

Question	Working	Answer	Mark	Notes
6	$28 \times 12 (=336)$ or $5 \times 12 (=60)$ or $18 \times 12 (=216)$ or $28 \times 20 (=560)$ or $\frac{1}{2} ("CD" + "18") "8"$ oe eg 72 $+4CD$ [numbers in “ ” come from correct working] Check diagram for areas $"336" + 0.5 ("18" + CD)"8" = 434$ oe eg $4("18" + CD) = 98$ or $eg 0.5("18" + CD)"8" = "98"$ oe eg $\frac{1}{2} ("CD" + "18") = 12.25$ or $"560" - 2(0.5(5 + x)"8") = 434$ oe (where x is horizontal from D to perp with AF) [numbers in “ ” come from correct working]		4	M1 For a correct method to find the area of a rectangle (may be seen as part calculation) or a correct expression for the area of the trapezium with numbers substituted. Allow for other correct method to find area linked to this shape. M1 correct use of their values from correct working for an equation involving CD (CD could be labelled with any letter)
	$eg (CD =) \frac{196 - 144}{8} (= \frac{52}{8})$ or $(CD =) \frac{98 - 72}{4} (= \frac{26}{4})$ or $(CD =) \frac{434 + 152 - 560}{4}$ or $(CD =) 2 \times 12.25 - 18$ or $98 \times (= 196), "196" \div 8 (= 24.5), "24.5" - 18$ <i>Correct answer scores full marks (unless from obvious incorrect working).</i>	6.5		M1 a correct process to solve a correct equation or a correct process to find CD using correct values
				A1 oe
				Total 4 marks

Question	Working	Answer	Mark	Notes
7 (a)		8	1	B1
(b)		11	1	B1 accept x^{11}
(c)		$8k^6m^{12}$	2	B2 for all correct B1 for two correct from 8 or k^6 or m^{12}
				Total 4 marks

Question	Working	Answer	Mark	Notes
8	1000 ($\div 60 \div 60$) or $\div 3600$ or sight of 81 000 or 1350 or 0.0225		3	M1 For one of $\times 1000$ (eg sight of 81 000) or ($\div 60 \div 60$) or $\div 3600$ oe
	$\frac{81 \times 1000}{60 \times 60}$ oe eg $\frac{81}{3.6}$ or $81 \times \frac{5}{18}$ oe			M1 For a fully correct method with correct use of brackets eg $81000 \div 60 \times 60$ is M1 only if not recovered
	Correct answer scores full marks (unless from obvious incorrect working).	22.5	A1	45 oe eg $\frac{45}{2}$
				Total 3 marks

Question	Working	Answer	Mark	Notes
9 (a)		$12a^{11}b^7$	2	B2 Fully correct (B1 for 2 correct terms in a product)
(b)		$7x^2y^2(2y^2 + 3x)$	2	B2 (B1 for a correct factorisation with at least 2 terms outside the bracket eg $xy(14xy^2 + 21x^2y)$ or for the correct common factor with only one error in the bracket)
(c)		$y = -2x + 4$	2	B2 for $y = -2x + 4$ oe (B1 for $y = -2x + c$ or clearly showing the gradient is -2 or $y = mx + 4$ or $-2x + 4$)
(d)		(0, -5)	1	B1
				Total 7 marks

Question	Working	Answer	Mark	Notes
10 (a)	$\sqrt{7.5^2 - 6^2}$ or $(BAC =) \sin^{-1} \left(\frac{6}{7.5} \right) (= 53.1)$ and $\frac{6}{\tan 53.1}$ " or $(BCA =) \cos^{-1} \left(\frac{6}{7.5} \right) (= 36.9)$ and $6 \times \tan 36.9$ "		2	M1 For a correct method to find AB
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	4.5		A1 oe
(b)	(area ABC =) $0.5 \times 6 \times "4.5"$ (= 13.5) oe (area ADC =) $31.5 - "13.5"$ (= 18) (AD =) $("18" \div 7.5) \div 0.5$ oe <i>Correct answer scores full marks (unless from obvious incorrect working).</i>		4	M1 ft their value of AB M1 For a method to find area ADC M1 For a complete method to find AD A1 cao
		4.8		
				Total 6 marks

Question	Working	Answer	Mark	Notes
11 (a)		$\frac{4}{10}, \frac{6}{10}$	1	B1 oe both probabilities correct.
(b)	$\frac{4}{11} \times \frac{3}{10}$		2	M1
(c)	$\frac{4}{11} \times \frac{7}{10}$ or $\frac{7}{11} \times \frac{4}{10}$ $\frac{4}{11} \times \frac{7}{10} + \frac{7}{11} \times \frac{4}{10}$	$\frac{12}{110}$	3	A1 oe $\frac{6}{55}$ oe eg 0.109.... M1ft Ft their tree diagram as long as given values are less than 1 M1ft
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$\frac{56}{110}$		A1oe $\frac{28}{55}$ oe eg 0.509....
				Total 6 marks

Question	Working	Answer	Mark	Notes
12 (a)	$(3x \pm 2y)(3x \pm 2y)$ or $(3x)^2 - (2y)^2$		2	M1
(b)	$\frac{7(4x)}{32x} - \frac{8(x+3)}{32x}$ or $\frac{7(4x)}{8(4x)} - \frac{8(x+3)}{8(4x)}$ or $\frac{28x}{32x} - \frac{8x+24}{32x}$ or $\frac{28x-8(x+3)}{32x}$ or $\frac{32x}{8x} - \frac{2(x+3)}{8x}$ or $\frac{7x-2(x+3)}{8x}$	$(3x+2y)(3x-2y)$	3	M1 for two correct fractions with common denominator or a single correct fraction
	$\frac{28x-8x-24}{32x}$ or $\frac{20x-24}{32x}$ or $\frac{7x-2x-6}{8x}$			M1 for correct fraction(s) with bracket(s) expanded and dealing with the negative signs
	$\frac{20x}{32x} - \frac{8x}{32x} - \frac{24}{32x}$			
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$\frac{5x-6}{8x}$		A1
				Total 5 marks

Question	Working	Answer	Mark	Notes
13 (a)	$(3x-1)(x+2) = 3x^2 + 6x - x - 2 (= 3x^2 + 5x - 2)$ or $(3x-1)(3x+1) = 9x^2 + 3x - 3x - 1 (= 9x^2 - 1)$ or $(x+2)(3x+1) = 3x^2 + x + 6x + 2 (= 3x^2 + 7x + 2)$ $[(3x^2 + 5x - 2)(3x+1) =] 9x^3 + 15x^2 - 6x + 3x^2 + 5x - 2$ or $[(9x^2 - 1)(x+2) =] 9x^3 + 18x^2 - x - 2$ or $[(3x^2 + 7x + 2)(3x-1) =] 9x^3 + 21x^2 + 6x - 3x^2 - 7x - 2$ <i>Correct answer scores full marks (unless from obvious incorrect working).</i>		3	M1 for a correct intention to multiply all 3 factors by multiplying 2 factors only, allow one error M1 (dep) ft for expanding by the third factor, allow one error
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i> ALTERNATIVE $9x^3 + 3x^2 + 18x^2 + 6x - 3x^2 - x - 6x - 2$	$9x^3 + 18x^2 - x - 2$		A1
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>		3	M2 for a complete expansion with 8 terms present, at least 4 of which must be correct
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$9x^3 + 18x^2 - x - 2$		A1
(b)	$(\frac{8xy^2}{2x^5})^2$ or $(\frac{x^4}{4y^2})^{-2}$ or $(\frac{4x^{10}}{64x^2y^4})^{-1}$ $(\frac{4y^2}{x^4})^2$ or $(\frac{x^8}{16y^4})^{-1}$ or $\frac{64x^2y^4}{4x^{10}}$ or $\frac{1}{64}x^{-2}y^{-4}$		3	M1 for one of reciprocating or simplifying or squaring M1 for two of reciprocating or simplifying or squaring
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$\frac{16y^4}{x^8}$		A1

ALTERNATIVE					$16y^4x^{-8}$ or $\frac{16}{y^{-4}x^8}$ or $\frac{16x^{-8}}{y^{-4}}$ oe
				3	M2 for 2 correct terms (M1 for 1 correct term)
			$\frac{16y^4}{x^8}$		A1 accept $16y^4x^{-8}$ or $\frac{16}{y^{-4}x^8}$ or $\frac{16x^{-8}}{y^{-4}}$ oe
					Total 6 marks

Question	Working	Answer	Mark	Notes
14 (a)		Fully correct Venn diagram	3	B1 For 13 correct in G only B2 For all 7 others correct (B1 for 4, 5 or 6 others correct (does not need to be complete for this))
(b)(i)		36	1	If these 3 parts are given as probabilities, please mark
(ii)		44	1	incorrect the first time but are present in
(iii)		35	1	ward marks from there on if the required numerator is correct regions
(c)		$\frac{18}{53}$	2	B2 ft oe 0.33(96...) or 33(.96...) % ft their Venn diagram or (B1 for $\frac{18}{m}$ where $m > 18$ or $\frac{n}{53}$ where $n > 53$ or for 18 : 53 or other incorrect notation) or B1 ft their Venn diagram for "18" where $m > "18"$ or $\frac{n}{53}$ where $n > "53"$
			Total 8 marks	

Question	Working	Answer	Mark	Notes
15	77.5 or 82.5 or 2.65 or 2.75 or 32.5 or 33.5 or 0.95 or 1.05 or 77500 or 82500 or 159 or 165 or 32500 or 33500 or 57 or 63		4	B1 For a UB or LB for one of the distances or times in hours or in minutes
	eg 82.5 \div 2.65 (= 31.13...) or 82500 \div 159 (= 518.867...) or km/min or m/h			M1 for a method to find the upper bound of Martin's average speed eg $UB_K \div LB_K$ where $80 < UB_K \leq 82.5$ and $2.65 \leq LB_K < 2.7$ or use of m/min to find upper bound for Martin's average speed eg $UB_K \div LB_K$ where $80\ 000 < UB_K \leq 82\ 500$ and $159 \leq LB_K < 162$ can use km/min or m/h
	eg 32.5 \div 1.05 (= 30.95...) or 32500 \div 63 (= 515.873.....) or km/min or m/h			M1 indep for a method to find the lower bound of Lucia's average speed eg $LB_S \div UB_S$ where $32.5 < LB_S \leq 33$ and $1 < UB_S \leq 1.05$ or use of m/min to find lower bound for Lucia's average speed $LB_S \div UB_S$ where $32\ 500 < UB_S \leq 33\ 000$ and $60 < UB_S \leq 63$ can use km/min or m/h
	$UB_K = 31132.....$ m/h $LB_S = 30952.....$ m/h	Shown		A1 shown with accurate figures in the same units – sufficient figures for comparison

Question	Working	Answer	Mark	Notes
17	$(\sqrt{2}-1)^2 = 2 - \sqrt{2} - \sqrt{2} + 1 (= 3 - 2\sqrt{2})$ $\frac{(3+\sqrt{8})^2}{(3-2\sqrt{2})} \times \frac{(3+2\sqrt{2})}{(3+2\sqrt{2})}$ eg $\frac{9+6\sqrt{2}+3\sqrt{8}+8}{9-6\sqrt{2}+-6\sqrt{2}-8}$ or $\frac{9+12\sqrt{2}+8}{9-8}$ or $\frac{9+6\sqrt{2}+3\sqrt{8}+8}{1}$ or $\frac{9+12\sqrt{2}+8}{1}$ <i>Working required</i>	$\frac{(3+\sqrt{8})^2}{(\sqrt{2}-1)^2} \times \frac{(\sqrt{2}+1)^2}{(\sqrt{2}+1)^2}$ $(\sqrt{2}-1)^2 = 2 - \sqrt{2} - \sqrt{2} + 1 (= 3 - 2\sqrt{2})$ or $(\sqrt{2}+1)^2 = 2 + \sqrt{2} + \sqrt{2} + 1 (= 3 + 2\sqrt{2})$ or $(\sqrt{2}+1)(\sqrt{2}-1) = 2 - \sqrt{2} + \sqrt{2} + 1 (= 1)$	4	M1 expand the denominator (accept $2 - 2\sqrt{2} + 1$ - must see expansion) or method to rationalise using $(\sqrt{2}+1)^2$ M1 oe ft $3 - 2\sqrt{2}$ method to rationalise or expansion of $(\sqrt{2}-1)^2$ (accept $2 - 2\sqrt{2} + 1$) or $(\sqrt{2}-1)^2$ (accept $2 + 2\sqrt{2} + 1$) or $(\sqrt{2}+1)(\sqrt{2}-1)$
		$17 + \sqrt{288}$		M1 dep on 2nd M1 correct expansion of brackets A1 or $p = 17, q = 288$ answer from fully correct working with intermediate steps of working seen
				Total 4 marks

Question	Working	Answer	Mark	Notes
18	$4x \times 2x - 2 \times \pi \times x^2 (= 20)$ oe or $2r \times 2r - \pi \times r^2 (= 10)$ oe $\sqrt{\frac{20}{8-2\pi}} (= 3.413\dots)$ or $\sqrt{\frac{10}{4-\pi}} (= 3.413\dots)$		4	M1 oe a correct expression or a correct equation for the shaded area (must be in one unknown only but x could be r or other letter)
	$\sqrt{\frac{20}{8-2\pi}} (= 3.413\dots)$ or $\sqrt{\frac{10}{4-\pi}} (= 3.413\dots)$ (perimeter =) $12 \times "3.413\dots"$ oe			M1 oe a correct expression for x or r or whatever letter is used
				M1 ft dep on first M1 For substituting values into a calculation for the perimeter use of their r or x
		41		A1 awrt 41
			Total 4 marks	

Question	Working	Answer	Mark	Notes
19	$(AD =) \frac{2.2}{\tan 18} (= 6.77\dots)$ or $(EA =) \frac{2.2}{\sin 18} (= 7.11\dots)$ $(DB =) \sqrt{6.77^2 + 6^2} (= 9.04\dots)$ or $(EB =) \sqrt{7.11^2 + 6^2} (9.31\dots)$ or $(EB =) \sqrt{6^2 + 6.77^2 + 2.2^2} (9.31\dots)$ $\tan DBE = \frac{2.2}{"9.04\dots"}$ or $\sin DBE = \frac{2.2}{"9.31\dots"}$ or $\sin DBE = \frac{2.2 \sin 90}{"9.31\dots"}$ $\cos DBE = \frac{"9.04\dots"}{"9.31\dots"}$ or use of cosine rule	13.7	4	M1 a correct method to find AD or AE M1 a correct method to find DB or EB M1 complete method to find one of $\tan DBE$ or $\sin DBE$ or $\cos DBE$ – NB: if using cosine, the student will need to have found DB and EB previously
	Correct answer scores full marks (unless from obvious incorrect working).			A1 Allow answers in range 13.59 – 13.8
				Total 4 marks

Question	Working	Answer	Mark	Notes
20	eg $-2(x^2 - 6x)$ oe		4	M1 for a correct factorisation of the expression involving the x parts
	eg $-2(x - 3)^2 \dots$ oe			M1 ft for starting the correct process to complete the square on their factorised expression – allow this mark even if the factorisation is incorrect
	eg $-2[(x - 3)^2 - 9] \dots$ oe			M1 ft for a complete process of completing the square for their factorised expression.
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$a = 25$ $b = 2$ $c = 3$		A1 oe allow $25 - 2(x - 3)^2$
				Total 4 marks

Question	Working	Answer	Mark	Notes
20 ALT	$a - bx^2 + 2bcx - bc^2$ oe or		4	M1 for correctly multiplying out $a - b(x - c)^2$
	$2bc = 12$ or $a - bc^2 = 7$ or $b = 2$			M1 for correctly equating coefficients
	For the correct values for 2 of a, b or c			M1 2 correct values from a or b or c
	<i>Correct answer scores full marks (unless from obvious incorrect working).</i>	$a = 25$ $b = 2$ $c = 3$		A1 oe allow $25 - 2(x - 3)^2$
				Total 4 marks

Question	Working	Answer	Mark	Notes
21	eg $\frac{20}{x^2-36} - \frac{2(x+6)}{x^2-36}$ oe or $\frac{20}{(x-6)(x+6)} - \frac{2(x+6)}{(x-6)(x+6)}$ oe or $\frac{20(x-6)}{(x^2-36)(x-6)} - \frac{2(x+6)(x-6)}{(x^2-36)(x-6)}$ or $\frac{20-2(x+6)}{(x^2-36)(4-x)}$ oe		3	M1 for writing the first two fractions with a common denominator (may be a single denominator) or multiplying both fractions by $\frac{1}{4-x}$ and writing over a common denominator
	eg $\frac{8-2x}{x^2-36} \times \frac{1}{4-x}$ or $\frac{8-2x}{(x+6)(x-6)} \times \frac{1}{4-x}$ or $\frac{20x-2x^2-48}{(x^2-36)(x-6)} \times \frac{1}{4-x}$ oe $\frac{8-2x}{(x^2-36)(4-x)}$ oe			M1 for simplifying first 2 fractions to a single fraction and expanding and simplifying numerator – must be correct, and showing intention to multiply by $\frac{1}{4-x}$ or expanding the numerator of the full solution and writing as a single fraction
	<i>Working required</i>	$\frac{2}{x^2-36}$		A1 oe eg $\frac{2}{(x+6)(x-6)}$ dep on M2
				Total 3 marks

Question	Working	Answer	Mark	Notes
22	$2 \times 3 \times 3 \times \left(\frac{3}{3^2} \right)^{4n+5}$ $\text{eg } \frac{2 \times 3 \times 3 \times \left(\frac{3}{3^2} \right)^{2(2n+8)}}{2 \times 3 \times 3 \times \left(\frac{3}{3^2} \right)^{2(2n+8)}} \text{ or } \frac{3 \times 3^{\frac{3}{2}(4n+6)}}{3^{2(2n+8)}}$ <p>$\sqrt{27}$ to be changed to a power of 3 and not $3\sqrt{3}$ unless recovered</p>		3	<p>M1 For 2 of:</p> <ul style="list-style-type: none"> writing 18 as 2×3^2 oe and 6 as 2×3 or cancelling 6 & 18 fully writing $\sqrt{27}$ as $3^{\frac{3}{2}}$ or $3 \times 3^{\frac{3}{2}}$ <p>or</p> <ul style="list-style-type: none"> $(\sqrt{27})^{4n+6}$ as $(3^3)^{2n+3}$ or 3^{6n+9} writing 9 as 3^2 or 9^{2n+8} as $3^{2(2n+8)}$ or 3^{4n+16}
	$\text{eg } \frac{3 \times 3^{6n+9}}{3^{4n+16}} \text{ or } \frac{3^{6n+10}}{3^{4n+16}} \text{ or } \frac{3 \times 3^{1.5(4n+6)}}{3^{2(2n+8)}} \text{ or } \frac{3^2 \times 3^{6n+9}}{3 \times 3^{4n+16}} \text{ or } \frac{3^{6n+11}}{3^{4n+17}} \text{ oe or } \text{eg } 3^{6n+11} = 3^x \times 3^{4n+17} \text{ oe}$ <p><i>Working required</i></p>			<p>M1 For a correct expression or equation using only powers of 3 (powers of 3 but not necessarily a single power)</p>
		$2n - 6$		A1 oe eg $2(n - 3)$ dep on M1
				Total 3 marks

Question	Working	Answer	Mark	Notes
23	$\frac{3}{5} = \frac{7-1}{8-k}$ oe eg $24 - 3k = 30$ $k = -2$ $\left(\frac{-2+8}{2}, \frac{1+7}{2}\right)$ oe or (3, 4) $\frac{3}{5}m = -1$ or $(m =) -\frac{5}{3}$ oe $"4" = "-\frac{5}{3}x" + c$ or $c = 9$ or $y - "4" = "-\frac{5}{3}(x - "3")$		6	M1 for correct equation linking the gradient to the given coordinates A1 for $k = -2$ M1 for finding the midpoint (use of their k where $k < 0$) M1 ft their gradient for use of $m_1 \times m_2 = -1$ Allow $-\frac{5}{3} = -1.67$ or better M1 dep on M3
	<i>Working required</i>	$5x + 3y = 27$		A1 allow equation in any form where p, q and r are integers
			Total 6 marks	